



Supervised Learning: Regression

Linear Regression

Description: Models the relationship between a dependent variable and one or more independent variables by fitting a linear equation to observed data.
Formula: $y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \dots + \beta_nx_n + \epsilon$
Assumptions: Linearity, independence, homoscedasticity, normality of residuals.
Use Cases: Predicting sales, estimating prices, forecasting demand.
Advantages: Simple, easy to interpret, computationally efficient.
Disadvantages: Sensitive to outliers, assumes linearity, can suffer from multicollinearity.
Regularization: Not inherently regularized. Use Ridge or Lasso for regularization.

Ridge Regression

Description: Linear regression with L2 regularization. Adds a penalty term equal to the square of the magnitude of coefficients.
Formula: Minimize $\sum_{i=1}^n (y_i - \beta_0 - \sum_{j=1}^p \beta_j x_{ij})^2 + \alpha \sum_{j=1}^p \beta_j^2$
Effect of α: Controls the strength of regularization. Higher α shrinks coefficients towards zero, reducing overfitting.
Use Cases: When multicollinearity is present, or to prevent overfitting.
Advantages: Reduces overfitting, handles multicollinearity better than linear regression.
Disadvantages: Requires tuning of the regularization parameter α , less interpretable than linear regression.

Lasso Regression

Description: Linear regression with L1 regularization. Adds a penalty term equal to the absolute value of the magnitude of coefficients.
Formula: Minimize $\sum_{i=1}^n (y_i - \beta_0 - \sum_{j=1}^p \beta_j x_{ij})^2 + \alpha \sum_{j=1}^p \beta_j $
Effect of α: Controls the strength of regularization. Higher α can lead to feature selection (some coefficients become exactly zero).
Use Cases: Feature selection, when many features are irrelevant.
Advantages: Performs feature selection, reduces overfitting, handles multicollinearity.
Disadvantages: Can arbitrarily select one feature among correlated features, requires tuning of the regularization parameter α .
Notes: L1 regularization.

Supervised Learning: Classification

Logistic Regression

Description: Models the probability of a binary outcome using a logistic function.
Formula: $p(y=1 x) = \frac{1}{1 + e^{-(\beta_0 + \beta_1x_1 + \dots + \beta_nx_n)}}$
Use Cases: Binary classification problems like spam detection, disease prediction.
Advantages: Simple, interpretable, provides probability estimates.
Disadvantages: Assumes linearity, can suffer from overfitting with high-dimensional data.
Regularization: Can be regularized using L1 or L2 regularization to prevent overfitting.

k-Nearest Neighbors (k-NN)

Description: Classifies data points based on the majority class among its k nearest neighbors.
Algorithm: - Choose the number of neighbors k. - Calculate the distance between the query point and all other data points. - Select the k nearest neighbors. - Assign the class label based on majority vote.
Use Cases: Recommendation systems, pattern recognition, image classification.
Advantages: Simple, no training phase, versatile.
Disadvantages: Computationally expensive, sensitive to irrelevant features, requires appropriate choice of k.
Distance Metrics: Euclidean, Manhattan, Minkowski.

Decision Trees

Description: A tree-like model that makes decisions based on features. Each node represents a feature, each branch represents a decision rule, and each leaf represents an outcome.
Splitting Criteria: Gini impurity, entropy, information gain.
Use Cases: Classification and regression tasks, feature selection, interpretable models.
Advantages: Easy to understand and interpret, handles both categorical and numerical data, can capture non-linear relationships.
Disadvantages: Prone to overfitting, can be sensitive to small changes in the data.
Ensemble Methods: Random Forests, Gradient Boosting.

Model Evaluation and Tuning

Evaluation Metrics

Accuracy: $\frac{\text{Number of Correct Predictions}}{\text{Total Number of Predictions}}$ Useful when classes are balanced.
Precision: $\frac{\text{True Positives}}{\text{True Positives} + \text{False Positives}}$ Ability of the classifier not to label as positive a sample that is negative.
Recall: $\frac{\text{True Positives}}{\text{True Positives} + \text{False Negatives}}$ Ability of the classifier to find all the positive samples.
F1-Score: $2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$ Weighted average of Precision and Recall.
ROC-AUC: Area Under the Receiver Operating Characteristic curve. Measures the ability of a classifier to distinguish between classes.
Confusion Matrix: A table summarizing the performance of a classification model.

Deep Learning Fundamentals

Core Concepts

Neural Networks: Models composed of interconnected nodes (neurons) organized in layers. Learn complex patterns through weighted connections and activation functions.
Perceptron: A single-layer neural network. Forms the basis for more complex networks.
Activation Functions: Introduce non-linearity to the network, enabling it to learn complex relationships. Examples: ReLU, sigmoid, tanh.
Backpropagation: An algorithm for training neural networks by iteratively adjusting the weights based on the error between predicted and actual outputs.
Loss Functions: Quantify the error between predicted and actual outputs. Examples: Mean Squared Error (MSE), Cross-Entropy.
Optimizers: Algorithms that update the network's weights to minimize the loss function. Examples: Adam, SGD, RMSprop.

Model Tuning

Cross-validation: A technique for evaluating model performance by partitioning the data into subsets for training and validation. Common methods include k-fold cross-validation.
Bias-variance tradeoff: Finding the right balance between bias (underfitting) and variance (overfitting) is crucial for model generalization.
Overfitting/underfitting: Overfitting: Model performs well on training data but poorly on unseen data. Underfitting: Model fails to capture the underlying patterns in the data.
Hyperparameter tuning: Optimizing model hyperparameters to improve performance. Techniques include GridSearchCV and RandomizedSearchCV.
GridSearchCV: Exhaustively searches through a specified subset of the hyperparameters.
RandomizedSearchCV: Randomly samples a given number of candidates from a parameter space.

Convolutional Neural Networks (CNNs)

Description: Specialized for processing structured array of data, such as images. Use convolutional layers to automatically learn spatial hierarchies of features.
Key Layers: Convolutional layers, pooling layers, fully connected layers.
Use Cases: Image classification, object detection, image segmentation.
Advantages: Efficiently captures spatial dependencies, robust to variations in position and scale.
Disadvantages: Can be computationally expensive, require large datasets.